Multilanguage Word Embeddings for Social Scientists: Estimation, Inference, and Validation Resources for 157 Languages^{*}

Elisa M. Wirsching[†] Pedro L. Rodriguez[‡] Arthur Spirling[§] Brandon M. Stewart[¶]

Abstract

Word embeddings are now a vital resource for social science research. However, obtaining high-quality training data for non-English languages can be difficult, and fitting embeddings therein may be computationally expensive. In addition, social scientists typically want to make statistical comparisons and do hypothesis tests on embeddings, yet this is non-trivial with current approaches. We provide three new data resources designed to ameliorate the union of these issues: (1) a new version of fastText model embeddings; (2) a multi-language "a la carte" (ALC) embedding version of the fastText model; (3) a multi-language ALC embedding version of the well-known GloVe model. All three are fit to Wikipedia corpora. These materials are aimed at "low resource" settings where the analysts lack access to large corpora in their language of interest or to the computational resources required to produce high-quality vector representations. We make these resources available for 40 languages, along with a code pipeline for another 117 languages available from Wikipedia corpora. We extensively validate the materials via reconstruction tests and other proofs-of-concept. We also conduct human crowdworker tests for our embeddings for Arabic, French, (traditional Mandarin) Chinese, Japanese, Korean, Russian, and Spanish. Finally, we offer some advice to practitioners using our resources.

^{*}The resources discussed in this paper can be found here: http://alcembeddings.org/

[†]PhD candidate, Wilf Family Department of Politics, New York University (elisa.wirsching@nyu.edu)

[‡]Visiting Scholar, Center for Data Science, New York University, United States; and International Faculty, Instituto de Estudios Superiores de Administración, Venezuela, (pedro.rodriguez@nyu.edu)

[§]Professor of Politics, Princeton University (as1780@princeton.edu)

[¶]Associate Professor, Sociology and Office of Population Research, Princeton University (bms4@princeton.edu)

Online Supporting Information: Multilanguage Word Embeddings for Social Scientists: Estimation, Inference, and Validation Resources for 157 Languages

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A Why fastText?

A strength of the fastText model is that it uses *subword* information when producing the embedding for a particular term (Grave et al., 2018). Rather than learning a single embedding vector for each whole word, fastText represents each word as a sum of the vector representations of its component parts. In practice, those components are *n*-gram contiguous characters, with special handling of word boundaries. This allows the technique to incorporate information about the internal structure of tokens.

Take, for example, a word like policies, and suppose n = 3. Then fastText would learn an embedding for pol, oli, lic, ici, cie, ies and one for policies itself. In addition, it would learn an embedding for the start and end of the word in the text, demarcating these as < and >. That is,

it also learns an embedding for <po and es>. A word is then represented by taking the *sum* of the vectors for each subword (plus the word itself and boundaries). In languages like Chinese, where words may be constructed of multiple logograms (themselves representing words), those individual characters are embedded and combined.

This can result in better predictions (and thus higher quality embeddings) because words that are not identical but that contain similar parts (like policy and policies) are not treated as completely separate entities. This is helpful when, say, a specific form of a word was rare (in the limit, absent) in the training documents but for which we still have some information from other more common tokens. This is also partly why the fastText technique is preferable to simply embedding the stems of terms. One can imagine that certain words with special meanings like "abortion" in US politics should not have the same representation as "abortive", even though their stem—"abort"—may be identical in some cases.

B GloVe embeddings

Global Vectors for Word Representation, known as GloVe (Pennington, Socher and Manning, 2014), are based on counts of word occurrence—that is, the frequency with which one word appears in a given window with (all) other words in a vocabulary. The co-occurrence count between words i and j is re-expressed as a probability of co-occurrence for i and j. Then the word vectors for i and j—the embeddings—are estimated such that multiplying them together (their dot product) comes as close as possible to reproducing that (log) probability of co-occurrence. This is done for all i and j, with some upweighting of probabilities where one has more data (i.e., where the underlying counts are higher). The technique can be applied to a local corpus and uses matrix factorization. Alternatively, users can download pre-existing GloVe embeddings fit to other corpora. These word vectors are then the *pre-trained* word embeddings for what follows.

C ALC embeddings

In the ALC settings, embeddings are derived from the additive information of pre-trained word embeddings (such as GloVe) in the context windows around the target word. However, simply averaging embeddings of context words over-emphasizes common words (e.g. "stop" words) (Khodak et al., 2018; Rodriguez, Spirling and Stewart, 2023). To produce "good" word representations, i.e. to recover existing word vectors $\mathbf{v}_{\mathbf{w}}$, one would therefore want to rotate away from such common components by multiplying the simple additive composition of embeddings \mathbf{u}_w with a "transformation matrix" \mathbf{A} .

$$\mathbf{v}_{\mathbf{w}} \approx \mathbf{A}\mathbf{u}_{\mathbf{w}} = \mathbf{A}\left(\frac{1}{|\mathbf{C}_{\mathbf{w}}|} \sum_{c \in \mathbf{C}_{\mathbf{w}}} \sum_{\mathbf{w}' \in c} \mathbf{v}_{\mathbf{w}'}\right)$$
(1)

with the set of contexts $\mathbf{C}_{\mathbf{w}}$ for word w, contexts c and context word embeddings $\mathbf{v}_{\mathbf{w}'}$. This yields an *approximation* to the "true" embeddings of the terms of interest but allows for high-quality "local" representations of terms in the relevant embedding space. In principle, this weighting matrix can be learned from the data by minimizing the error between existing word vectors (locally trained or relying on large pre-trained corpora) and their respective additive context embeddings:

$$\hat{\mathbf{A}} = \arg\min_{\mathbf{A}} \sum_{w=1}^{W} \alpha(n_w) \|\mathbf{v}_w - \mathbf{A}\mathbf{u}_w\|_2^2$$
(2)

Here $\alpha(n_w)$ weights up words (embeddings) that are more common in the corpus and about which we have more information. This equation is a simple linear regression problem, and learning the transformation matrix is not particularly hard. What makes it difficult in practice is obtaining data on which to estimate **A**. We use Wikipedia for this purpose and thus provide the transformation matrix for every language we processed so far.

D Details on Training Process

D.1 Wikipedia Corpora

As the largest free online encyclopedia, available in more than 200 languages, Wikipedia provides an important resource for multilanguage natural language processing. Importantly, because the articles are curated, the underlying text corpora are of high quality, and the corpora ensure broad coverage in terms of topics and content. We downloaded the XML Wikipedia dumps for each language¹, using the latest month available at the time of the respective download.² Table 3 depicts the size of the Wikipedia corpora by language. Evidently, the size of the training corpora used for our resources vary substantially and—as Figure 3 indicates—the ability of ALC to reconstruct the underlying pre-trained **fastText** embeddings correlates positively with the size of the training corpora across languages. Especially scholars working in languages with smaller Wikipedia corpora should, therefore, carefully assess the fit of our resources and compare them against a local fit of ALC embeddings.

¹https://dumps.wikimedia.org/

 $^{^{2}}$ See the code pipeline for the specific corpora used.

| Language | Number of tokens | Number of types |
|-----------------------|------------------|-----------------|
| English (en) | 2509107528 | 487548 |
| German (de) | 909529231 | 741082 |
| Japanese (ja) | 822043573 | 168054 |
| French (fr) | 814072051 | 393310 |
| Spanish (es) | 708130887 | 331604 |
| Russian (ru) | 544851977 | 556247 |
| Italian (it) | 521266262 | 303043 |
| Mandarin (zh) | 415856806 | 131437 |
| Portuguese (pt) | 307958805 | 279710 |
| Dutch (nl) | 280699206 | 269485 |
| Ukrainian (uk) | 252927316 | 331524 |
| Polish (pl) | 252015897 | 316233 |
| Catalan (ca) | 230276780 | 247556 |
| Swedish (sv) | 198491360 | 257251 |
| Arabic (ar) | 191722613 | 322748 |
| Hebrew (he) | 145225021 | 284314 |
| Vietnamese (vi) | 142363557 | 182936 |
| Czech (cs) | 141914459 | 314574 |
| Hungarian (hu) | 117150915 | 325888 |
| Indonesian (id) | 105720582 | 108170 |
| Norwegian (no) | 102522025 | 204184 |
| Finish (fi) | 86744273 | 325253 |
| Korean (ko) | 85540639 | 368452 |
| Greek (el) | 84863862 | 217338 |
| Romanian (ro) | 79237177 | 197309 |
| Bulgarian (bg) | 67922614 | 197136 |
| Danish (da) | 58681996 | 188904 |
| Egyptian Arabic (arz) | 48966691 | 151983 |
| Slovenian (sl) | 42813035 | 185169 |
| Bengali (bn) | 39265385 | 133407 |
| Hindi (hi) | 35477207 | 88619 |
| Slovakian (sk) | 34544078 | 178530 |
| Estonian (et) | 33762935 | 210219 |
| Urdu (ur) | 31543933 | 65331 |
| Lithuanian (lt) | 26653065 | 151937 |
| Latvian (lv) | 18603697 | 109113 |
| Swahili (sw) | 6909049 | 32927 |
| Irish (ga) | 6271469 | 55815 |
| Kmer (km) | 5782880 | 37318 |
| Maltese (mt) | 2509660 | 44685 |

Table 3: Size of Wikipedia corpora by language. All corpora have been preprocessed according to our guidelines in Appendix D.2.

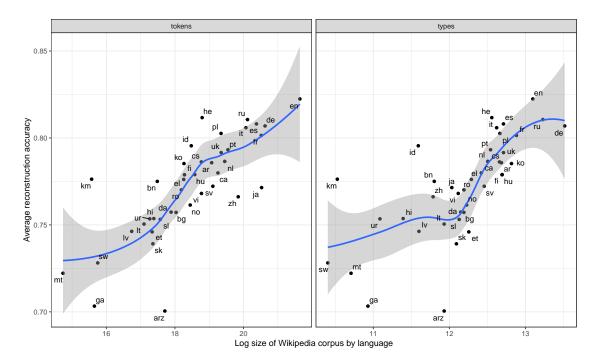


Figure 3: Relationship between size of Wikipedia corpus (number of tokens or types) and reconstruction accuracy as shown in Figure 1.

D.2 Preprocessing Choices

The first preprocessing step is to extract the text content from the XML dumps. For this purpose, we follow the fastText pipeline and use the WikiExtractor from apertium³. In a second step, we implement light preprocessing of the resulting corpora. In particular, we removed punctuation (except for punctuation within tokens), removed extra white space, and set all characters to lower case. Finally, we tokenize the raw text. As before, we largely follow choices made by the original fastText (Grave et al., 2018) to ensure better comparability of our models with existing options. We use the Stanford word segmenter for Chinese (Chang, Galley and Manning, 2008) and Mecab for Japanese (Kudo, 2005). For languages written using the Latin, Cyrillic, Hebrew or Greek scripts, we use no separate tokenizer, but split based on white space. For all remaining languages, we use the ICU tokenizer (Rui, 2020).

Additionally, when training the models (fastText, GloVe and their respective ALC embeddings), we apply a hard minimal frequency threshold for the respective vocabulary. This helps to clean out noisy parts of the corpus and thus significantly improves the fit of all models. We base our choice on the language-specific threshold on the size of the Wikipedia corpora and vocabulary by language⁴. Specifically, we impose a minimal frequency cutoff of 50 for English, 25 for medium-sized languages (i.e., German, Spanish, Italian, French, Russian, Swedish, and Dutch), 15 for small-to-medium-sized languages (i.e., Czech, Finish, Hungarian, Portuguese) and 10 for all smaller languages. As this step turned out to be crucial for the out-of-sample performance of our quantities, scholars who use our code pipeline to train resources from Wikipedia for their language

³https://github.com/apertium/WikiExtractor

⁴https://meta.wikimedia.org/wiki/List_of_Wikipedias

might want to experiment with the size of the threshold in their particular case.

Note that the crowdsourcing validation in the main text was done with a previous version of our resources. Following internal experiments and out-of-sample performance tests, we adjusted preprocessing and training choices after our crowdsourcing survey. Table 4 details the exact differences across the two iterations of our resources.

| Category | Current Resources (as of June 2023) | Previous Resources (Crowdsourcing) |
|-------------------|---------------------------------------------------------|------------------------------------|
| Preprocessing | • Remove punctuation btw tokens (i.e. emulate quanteda) | • Remove <i>all</i> punctuation |
| | • Remove extra white space | • Remove extra white space |
| | • Set characters to lower case | • Set characters to lower case |
| | | • Remove numbers |
| GloVe training | • Vector size: 300 | • Vector size: 300 |
| | • Window size: 5 | • Window size: 5 |
| | • Vocab min count: language-specific | • Vocab min count: 5 |
| | • x_{max} in weighting: 100 | • x_{max} in weighting: 10 |
| | • Maximum iterations: 50 | • Maximum iterations: 10 |
| fastText training | • Skip-gram model | • CBOW model |
| | • Vector size: 300 | • Vector size: 300 |
| | • Window size: 5 | • Window size: 5 |
| | • Vocab min count: language-specific | • Vocab min count: 5 |
| | • Negative sampling: 10 | • Negative sampling: 10 |
| ALC | • Vocab min count: language-specific | • Vocab min count: 10 |

Table 4: Changes in training procedure across iterations of ALC resources.

D.3 Training of fastText Embeddings

Next, we train fastText models (Grave et al., 2018) for this preprocessed and tokenized text using a context window of 5 and setting the dimensions of the word vectors to 300. For the dictionary, we impose the minimal frequency of occurrences in the entire corpus described in Section D.2 and use negative sampling of size 10.

D.4 Training of GloVe Embeddings

Similarly, we train GloVe (Pennington, Socher and Manning, 2014) to our cleaned corpora. Again, we set a language-specific minimal word frequency described in Section D.2, a vector size of 300, and a context size of 5. We further impose similar parameters as in Pennington, Socher and Manning (2014), i.e., we set $x_m ax = 100$, $\alpha = 3/4$ and a maximum iteration of 50.

D.5 Training of ALC Embeddings

Finally, for both fastText and GloVe embeddings, we then train ALC embeddings (Khodak et al., 2018; Rodriguez, Spirling and Stewart, 2023) to obtain the relevant transformation matrices. We use a chunk-based learning approach to handle the large size of the respective corpora. That is, we read in the relevant preprocessed corpus by chunk and perform the following operations by chunk:

1. Retain vocabulary with a minimum term frequency of the language-specific threshold

- 2. Create a feature-cooccurrence-matrix (FCM) using conText⁵, with a window size of 5 and equal weighting
- 3. Obtain a corresponding feature-embedding-matrix that provides additive context-specific feature embeddings (i.e., the $\mathbf{u}_{\mathbf{w}}$ in Equation (1)), averaged over all embedding instances in a given chunk

To obtain the untransformed additive embeddings for all features across the *entire* corpus, we then simply average the chunk-specific additive embeddings for each feature across the chunks. This is possible because the additive context embeddings from step 3 are themselves averages of the respective instance-specific additive context embeddings in a given chunk. We do this for all features appearing with a frequency of at least the language-specific threshold across the entire corpus. Finally, we train the corresponding transformation matrix following Equation (2), where we use $\log(n_w)$ for $\alpha(n_w)$.

E Reconstruction Tests: Full Description

To fix ideas, suppose we are working with Spanish and have Spanish Wikipedia as our large, pretraining corpus (~ 639 million tokens, ~ 850 thousand types). We proceed as follows:

- 1. Draw 100 random terms from the corpus. The only requirement on these terms is that they have higher frequency counts than the median token in the corpus.
- 2. Putting those 100 terms aside, produce embeddings for the large corpus via our cleaned version of fastText and GloVe. Thus we have two sets of "true" embeddings.
- 3. Estimate an A matrix in the usual ALC way for both architectures' embeddings.
- 4. For the 100 held-out terms for both architectures, produce an ALC embedding for each term.
 - (a) For any given random term, say pulpo (Spanish for octopus), we now have an ALC embedding from fastText and from GloVe.
 - (b) Calculate the cosine similarity between our ALC embedding of pulpo from fastText and the "true" fastText embedding; calculate the cosine similarity between our ALC embedding of pulpo from GloVe and the "true" GloVe embedding.
- 5. Repeat steps 4a and 4b for all of the 100 random held out words. Calculate the mean cosine distance from the "true" embeddings.

F English-Spanish "translation" at the European Parliament

We want to check that words represented via our embeddings "mean" what we expect them to. We verify this by studying a curated domain setting—specifically, translated English/Spanish speeches at the European Parliament (EP), 1999–2001 (Høyland, Sircar and Hix, 2009). To summarize: first, we produce an 'English' corpus of speeches either originally in English or translated from

⁵https://github.com/prodriguezsosa/conText

Spanish to English. Then, we produce a 'Spanish' corpus of speeches either originally in Spanish or translated from English to Spanish.

More specifically, for the English and Spanish speech data in Høyland, Sircar and Hix (2009), we proceed as follows:

- 1. Gather all speeches originally in English in the EP (denote as en_orig), and obtain their (expert) translation to Spanish (en_to_es).
- 2. Gather all speeches originally in Spanish in the EP (es_orig), and obtain their (expert) translation to English (es_to_en).
- 3. Combine en_orig and es_to_en into one English corpus. Use ALC to obtain the nearest neighbors of the word also. Compare the cosine similarity ratio (en_orig es_to_en) for each nearest neighbor to also.
- 4. Combine es_orig and en_to_es into one Spanish corpus. Use ALC to obtain the nearest neighbors of the word también. Compare the cosine similarity ratio (<u>en_to_es_orig</u>) for each nearest neighbor to también (the Spanish translation of but).

The results of this exercise for the two corpora are displayed in Figure 4. We use different plotting figures to denote whether the nearest neighbor in question is from the Spanish corpus only, shared between the corpora, or from the English corpus only. To understand the figure, start with the left panel—the combined English corpora. If we assume that (a) politicians whose native languages differ (English or Spanish) do not use **also** in systematically different ways and (b) that translation is noiseless (perfect), then we would anticipate that the cosine ratio for the nearest neighbors will be 1. That is, we anticipate that, say, a term like **because** (its embedding) will be as close to **also** in the original English corpus as in the *translated to* English corpus. This is, in fact, what we see. Furthermore, we see it for all the top 10 nearest neighbors. Turning to the right part of the plot, and with evidence in hand that assumptions (a) and (b) hold from the left panel, we would hope that the nearest neighbors for **también** will also line up at 1. If they do, we have evidence that ALC "works" for Spanish—that is, it produces reasonable nearest neighbors for terms we might care about, with which professional translators would concur. This is precisely what we see.

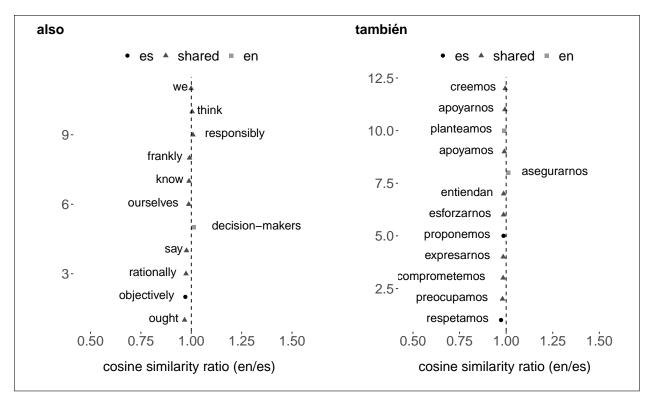


Figure 4: Translation Exercise: Cosine Similarity Ratio for ALC Nearest Neighbors is almost always 1 for translated and original texts in English and Spanish.

Notice that the embeddings themselves are *not* being translated between English and Spanish. Indeed, a feature of our multilanguage representations is that they inhabit different spaces (one per language). Our point here is that a technique (ALC) we believe works for English also works for other languages (in this case, Spanish).

G Multilanguage Crowdsourcing Details

For the crowdsourcing validation of our resources, we first employ the three embedding models we aim to compare (the original fastText embedding model from (Grave et al., 2018), our fastText model trained on Wikipedia and our ALC model using our fastText model for the underlying pre-trained embeddings) to obtain the top 20 nearest neighbors in the seven relevant languages for the eight political keywords (law, liberty, equality, justice, politics, tax, citizen, police) using our Wikipedia corpora. Following Rodriguez and Spirling (2022), we build a simple app that prompts crowdworkers to compare the nearest neighbors for these models. After a short introduction of the task and the general idea of keywords and context words, we ask crowdworkers to indicate which model produces nearest neighbors that best meet the definition of a context word (Figure 5 shows the task description in English). For this, we use pairwise comparisons, i.e., a given crowdworker either compares (1) the original fastText model to our fastText model or (2) our ALC model to our fastText model. Instead of showing the crowdworkers *all* nearest neighbors for a given keyword across the two models in the comparison, we randomly select a nearest neighbor from each set of the 20 nearest neighbors. To rule out ties, we also remove draws where nearest neighbors are identical across the two models in the comparison. We then translate the app for all relevant seven languages with the help of native speakers. Figure 6 shows an example of a pairwise comparison for police in Japanese and tax in Russian. In collaboration with $CloudResearch^6$, we then field these apps in the following regions, recruiting 50 crowdworkers for each language:

- Arabic: Saudi Arabia, Egypt, Algeria
- Chinese (traditional): Taiwan
- French: France, Canada (Quebec)
- Japanese: Japan
- Korean: South Korea
- Spanish: Mexico, Costa Rica, Colombia
- Russian: Russia, Belarus

⁶https://www.cloudresearch.com/

Context Words

A famous maxim in the study of linguistics states that: You shall know a word by the company it keeps. (Firth, 1957) This task is designed to help us understand the nature of the "company" that words "keep": that is, their CONTEXT.

Specifically, for a CUE WORD, its CONTEXT WORDS include words that:

• Tend to occur in the vicinity of the CUE WORD. That is, they are words that appear close to the CUE WORD in written or spoken language. AND/OR

• Tend to occur in similar situations to the CUE WORD in spoken and written language. That is, they are words that regularly appear with other words that are closely related to the CUE WORD.

For example, CONTEXT WORDS for the cue word COFFEE include:

cup (tends to occur in the vicinity of COFFEE).
 tea (tends to occur in similar situations to COFFEE, for example when discussing drinks).



(a) General Introduction

Task Description

For each iteration of the task (13 in total including trial and screener tasks):

1. You will be given a cue word (top center of the screen) and two candidate context words (on either side of the cue word).

2. Please select the candidate context word that you find best meets the definition of a context word.

3. We are especially interested in context words likely to appear in **political discourse.**

4. If both are reasonable context words, please select whichever you find most intuitive.

5. You must select **one and only one** of the two candidate context words.

Keep in mind, some iterations are for screening purposes. These are tasks for which there is clearly a correct answer.

Wrong answers in these screening tasks will automatically end your participation so be sure to read carefully.

The trial task that follows is meant for you to practice. Like screening tasks, the trial task has a correct answer.

Click "Next" to continue to the trial runs



(b) Task Description

Figure 5: Crowdsourcing Instructions

練習1/10



НАЛОГ



Выберите наиболее подходящее контекстное слово для ключевого слова, установив соответствующий флажок под словом.

Нажмите «Далее», чтобы продолжить

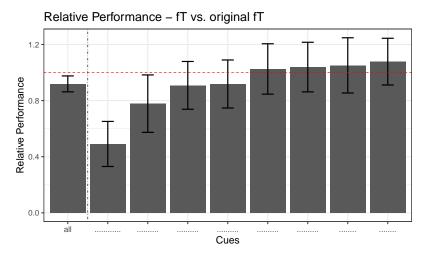
Далее

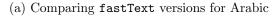
(b) Example of Pairwise Comparison in Russian

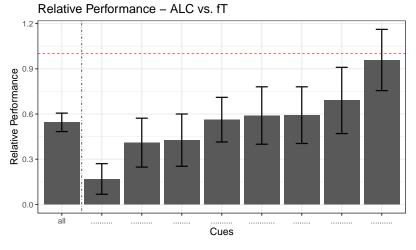
Figure 6: Crowdsourcing Examples

H Full Crowdsourcing Results: Model v Model

H.1 Arabic



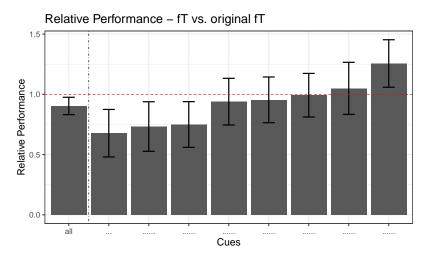


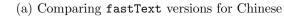


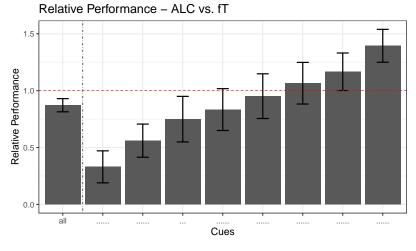
(b) Comparing fastText and ALC for

Figure 7: Summary of crowdsourcing comparisons for Arabic.

H.2 Chinese (Mandarin)



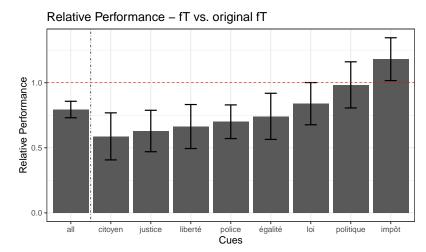


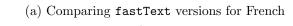


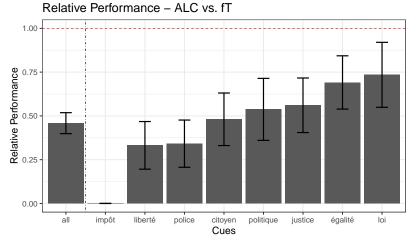
(b) Comparing fastText and ALC for Chinese

Figure 8: Summary of crowdsourcing comparisons for Chinese (Mandarin)

H.3 French



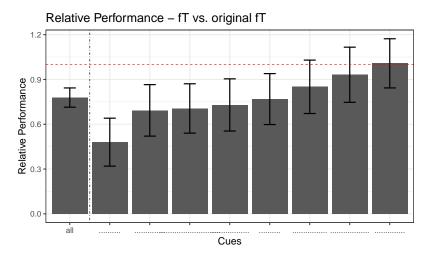


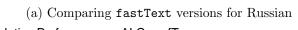


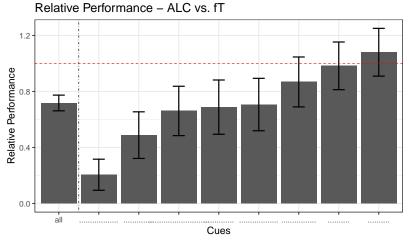
(b) Comparing fastText and ALC for French

Figure 9: Summary of crowdsourcing comparisons for French.

H.4 Russian



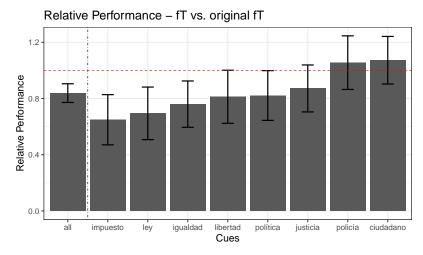


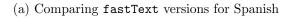


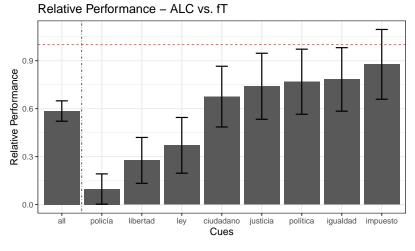
(b) Comparing fastText and ALC for

Figure 10: Summary of crowdsourcing comparisons for Russian.

H.5 Spanish







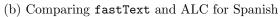
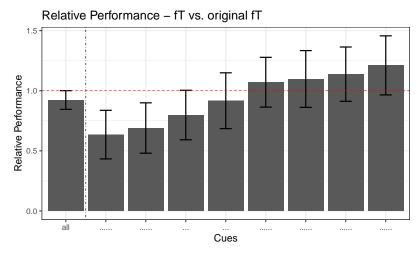
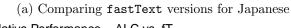
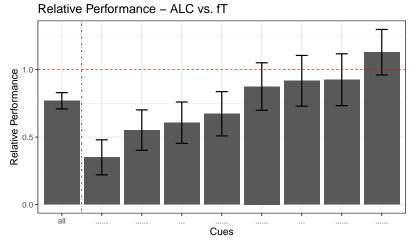


Figure 11: Summary of crowdsourcing comparisons for Spanish.

H.6 Japanese







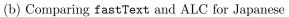
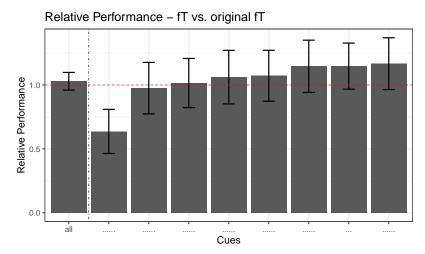
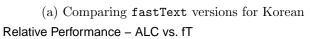
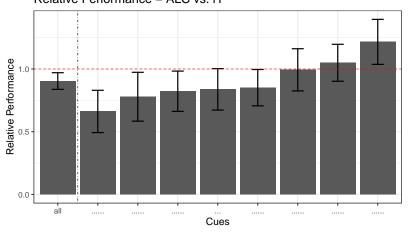


Figure 12: Summary of crowdsourcing comparisons for Japanese.

H.7 Korean







(b) Comparing fastText and ALC for Korean

Figure 13: Summary of crowdsourcing comparisons for Korean.

I Robustness of Validation Tests

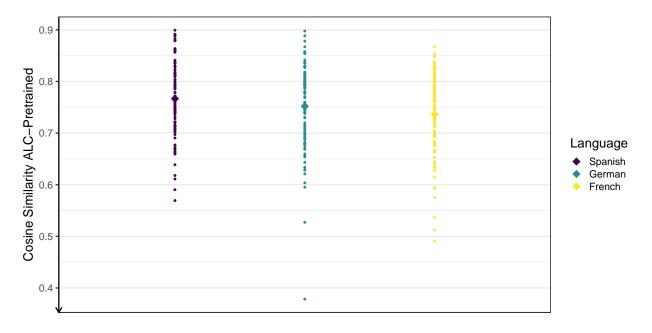


Figure 14: Reconstruction performance: cosine similarity between our ALC version of fastText those underlying architectures for 100 random terms at the 25th percentile of the type distribution. Languages are ordered according to the mean accuracy for fastText. In theory, cosine similarities range between -1 and 1, but empirically all estimates are positive.

| democracy | | equality | |
|------------------|------------------------------------|---------------------|---------------------|
| our fT | our fT-ALC | our fT | our fT-ALC |
| democratization | democratising | non-discrimination | non-discrimination |
| social-democracy | internationalism | anti-discrimination | inclusiveness |
| e-democracy | parliamentarism | anti-discriminatory | antidiscrimination |
| socialism | $\operatorname{constitutionalism}$ | inclusiveness | anti-discrimination |
| democratising | democratisation | inequality | anti-discriminatory |

Table 5: Nearest neighbors for English terms democracy and equality.

| nationalisme | | racisme | |
|---------------------|---------------------|---------------|----------------------------------|
| our fT | our fT-ALC | our fT | our fT-ALC |
| néonationalisme | l'internationalisme | antiracisme | l'antiracisme |
| régionalisme | internationalisme | l'antiracisme | $\operatorname{communautarisme}$ |
| internationalisme | radicalisme | l'homophobie | antiracisme |
| l'internationalisme | néonationalisme | xénophobie | l'islamophobie |
| traditionalisme | progressisme | sexisme | d'islamophobie |

Table 6: Nearest neighbors for French terms nation and racisme.

J Approximately In Sample

Suppose the researcher's local corpus is "close enough" to Wikipedia. In that case, using our prefitted transformation matrix will work as well as anything else from the perspective of producing ALC embeddings. Inevitably, there is ambiguity in "close enough", but one way to diagnose whether this is true is to, e.g., inspect the nearest neighbors and compare them to the researcher's substantive priors.

To give an example of a limiting case (i.e., being as close as possible to the training data), we illustrate the capacity of ALC to identify homonyms. These terms have identical spelling across contexts but different meanings. For instance, the German term kiefer means both pine and jaw, and the term **erde** can imply both **Planet Earth** and **soil**. If ALC works well with corpora that are close to or identical to Wikipedia, we would expect the context-specific embeddings to uncover these differences in meaning across contexts. As Table (7) and Figure (15) indicate, this is the case. We embed each instance of the terms kiefer and erde à la carte by applying our fastText quantities (pre-trained embeddings and transformation matrix) to the German Wikipedia. We cluster these ALC embeddings using k-means (for k = 2). Table (7) shows the nearest neighbors to the center of each cluster. Evidently, the first cluster of kiefer contains terms related to teeth and jaw bone, while the second cluster only includes other tree species, such as larch (lärche) or spruce (fichte). Similarly, the first cluster of erde captures terms such as vegetation cover (planzendecke) and rocks (gesteinsbrocken). In contrast, the second cluster is most closely related to words relevant to planet, sun, or moon. Given these patterns, it is not surprising that these ALC clusters are also well-separated in two principal component dimensions (Figure (15))—note the homogeneity of the word senses, with relatively little overlap on the first dimension.

| kiefer | | erde | |
|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------|-----------------------------------------------------------------------------------------------------------------------------------------------|---------------------------------------------------------------------------------------------------------------------------------------------------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| Cluster 1 | Cluster 2 | Cluster 1 | Cluster 2 |
| scherengebiss praemaxillare protraktil oberkieferknochen kieferknochen pharyngealia schläfenbein zwischenkieferbein oberkiefers gaumenbein | fichten nadelbaumarten waldkiefer schwarzkiefer lärche weißtanne weymouth-kiefer douglasie weiß-tanne balsam-tanne | erde erdklumpen erdnester gesteinsbrocken waldboden pflanzendecke lufthülle vegetationsdecke menschenhand menschenwelt | himmelskörpers magnetosphäre planetenoberfläche sonnenoberfläche sonnennähe meteoroiden sonnensystems erde-mond äquatorebene himmelskörpern |

Table 7: Nearest neighbors to ALC clusters of German homonyms kiefer and erde.

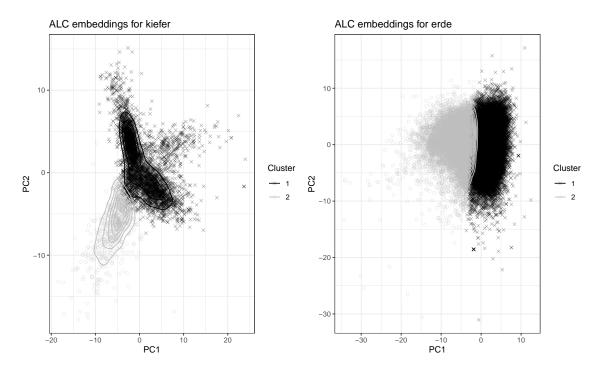


Figure 15: Identification of clusters in German homonyms kiefer (pine, jaw) and erde (Earth, soil).

K Out of Sample, "Small" Corpus

We use parliamentary corpora from the French and Italian parliamentary debates, as compiled by the *ParlaMint* project (Erjavec et al., 2023). In both examples, we use our pre-trained fastText embeddings together with the corresponding transformation matrices trained on Wikipedia. The first example uses the parliamentary minutes from the French National Assembly (Assemblée Nationale) for 2019-2020, which yields a corpus of about 216,000 documents. We show how ALC can capture changes in the meaning of certain keywords over time, specifically, how the connotation of liberty changes in French parliamentary debates before and after the Covid-19 outbreak. Figure (16) shows the average cosine similarity between ALC embeddings for liberté and our fastText pre-trained embeddings for relevant terms, including pluralisme (pluralism), urgence (emergency) and visite (visit). As one would expect, the figure shows how the usual nearest neighbors of liberté, i.e., pluralisme, équité and discrimination, experience a sharp drop in their cosine similarity with the ALC embedding of liberté. In contrast, a priori less closely related terms, such as covid, urgence and visite, show a substantially larger cosine similarity with liberté once the virus became a major health crisis in France. These dynamics were particularly stark in April 2020, when the Covid cases reached their first peak and the French government enacted a strict lockdown.

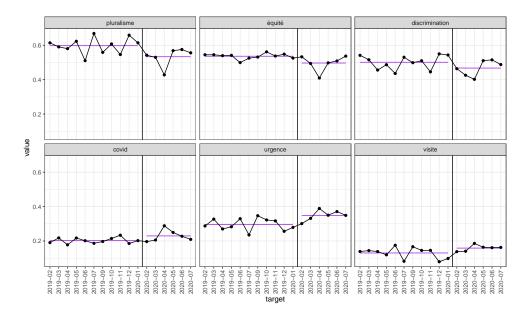
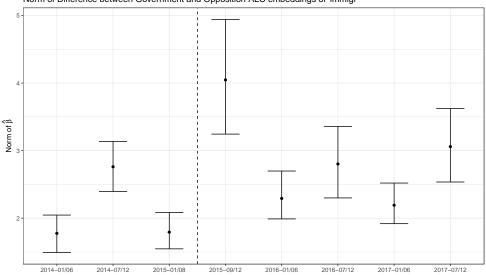


Figure 16: Average cosine similarity between ALC embeddings of liberté and pre-trained embeddings of relevant terms by month.

The second example uses embedding regressions to illustrate how the 2015 refugee crisis in Europe altered partian differences in debates around immigration issues in Italy's federal parliament. Using text from all parliamentary speeches for 2014-2017 (N = 20,747), we regress the ALC embeddings for immigration-related terms (i.e., immigrati, immigrazione, immigrato, immigrate, immigrazioni) across 6-month periods on a binary indicator for whether the speaker's party is part of the government or opposition. The multivariate regression analogy is

$$\mathbf{Y} = \beta_0 + \beta_1 Government + \mathbf{E} \tag{3}$$

Figure (17) depicts the norm of β_1 for each period. When the estimate increases, this indicates that the use of immigr* becomes less similar across government and opposition parties. The estimates show that speakers from different parliamentary camps differ throughout the entire period, and most strongly in the months between September and December 2015—a period with large and unexpected waves of refugees arriving in Southern Europe. Figure (18) further highlights that this discontinuity in semantic differences is indeed meaningful. The figure shows terms that are most closely related to opposition and government parties in relation to immigration issues before and after the large influx of refugees. Specifically, we show the cosine similarity ratio of the ALC embeddings for immigration-related terms across opposition and government parties shortly before (subfigure (a)) and after (subfigure (b)) the refugee crisis began. In early 2015, both types of parliamentary camps discussed issues of immigration in similar ways, often sharing nearest neighbors such as emergency (emergenziale) or applicants (richiedenti). In the later months of 2015, in contrast, the vocabularies radically differ between government and opposition parties. While opposition parties still seem to talk about immigration in more general terms (e.g., invoking terms lexically related to immigrazione), government parties now mention normative challenges of immigration as well as legal constraints, e.g., the Schengen area or the "Bossi-Fini law". It is worth noting that we excluded stop words from the Italian parliamentary corpus to improve the performance of ALC in this case. It is possible that excluding stop words can "help" the transformation matrix in screening out common directions in the embedding space, and users may want to test the importance of removing vs. keeping stop words in their relevant language and use case. Taken together, these two examples across different parliamentary settings highlight the power of ALC to capture and illustrate semantic differences across time and groups.



Norm of Difference between Government and Opposition ALC embeddings of 'immigr*'

Figure 17: Relative semantic shift of immigr* between government and opposition parties.



Figure 18: Discussion of immigration diverged between government and opposition parties after the 2015 European refugee crisis

Readers may reasonably ask whether fitting the **A** matrix locally in this case would have resulted in "better" (more locally precise) embeddings. Our answer here is "no", as Table (8) shows. The table compares our pre-trained quantities and their application with locally trained embeddings to the French parliamentary debates. Columns 1 and 3 list the nearest neighbors for liberté for the pre-trained embeddings (our fastText and locally trained GloVe), and columns 2 and 4 show the nearest neighbors for the corresponding ALC embeddings of liberté. Evidently, our fastText resources capture meaningful connotations of the keyword, both for pre-trained and ALC embeddings. In contrast, locally trained quantities work well for GloVe but not for its ALC version. That is, inspecting column 4, we see that the nearest neighbors for the ALC embedding of liberté depict only function words, such as encore or aussi. Note that we excluded stop words in the underlying parliamentary corpus (except for the training of the GloVe model) to facilitate a better local fit. So, while our general suggestion is to fit the relevant quantities locally if the corpus is large enough, in this particular case, that size requirement was not fulfilled.

| our fT | our fT-ALC | local GloVe | local GloVe-ALC |
|----------------|-------------------------------------|--------------|-----------------|
| liberté | l'irresponsabilité | liberté | aussi |
| libertés | non-discrimination | d'expression | c'est |
| d'expression | l'impartialité | droit | surtout |
| démocratie | d'impartialité | contraire | aujourd'hui |
| conditionnelle | pluralisme | principe | tout |
| légalité | légalité | choisir | car |
| pluralisme | l'exigence | respect | bien |
| laïcité | d'autrui | doit | enfin |
| dignité | contrevient | toute | seulement |
| l'égalité | $l'in constitution na lit\acute{e}$ | cause | fait |

Table 8: Nearest neighbors for liberté for different pretrained embeddings and transformation matrices. The ALC embeddings, and the local GloVe model, use the French parliamentary corpus from Erjavec et al. (2023), 2017-2020.

To illustrate this later point, we juxtapose our results in Table 8 with a parallel exercise with the ALC embeddings for the term **freedom** using the Congressional records (Session 111-114) (Gentzkow, Shapiro and Taddy, 2018) in Table 9. Evidently, all sets of embeddings, i.e., the **fastText** pre-trained embeddings, the locally trained **GloVe** embeddings, and their respective ALC embeddings, return meaningful and very similar nearest neighbors for **freedom**. This implies that the locally fit quantities do not lag behind the pre-trained resources, provided the local corpus provides sufficient data to estimate high-quality embeddings and transformation matrices.

| our fT | our fT-ALC | local GloVe | local GloVe-ALC |
|--------------|-----------------|-------------|-----------------|
| freedom | freedom | freedom | freedom |
| freedoms | conscience | liberty | liberty |
| liberty | civility | rights | rights |
| liberties | freedoms | free | freedoms |
| equality | liberties | freedoms | religious |
| conscience | democracy | religious | free |
| democracy | humanitarianism | nation | fundamental |
| secularism | compassionately | citizens | democracy |
| independence | equality | world | citizens |
| rights | uscirf | right | principles |

Table 9: Nearest neighbors for **freedom** for different pretrained embeddings and transformation matrices. The ALC embeddings and the local **GloVe** model use the Congressional corpus from Gentzkow, Shapiro and Taddy (2018).

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